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Working Paper 16/251  
November 2016

Economics Working Paper Series

**ETH**

Eidgenössische Technische Hochschule Zürich  
Swiss Federal Institute of Technology Zurich

# Persistent and Transient Cost Efficiency—An Application to the Swiss Hydropower Sector

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This draft version: November 16<sup>th</sup> 2016

## Abstract

Electricity prices on the European market have decreased significantly over the past few years, resulting in a deterioration of Swiss hydropower firms' competitiveness and profitability. One option to improve the sector's competitiveness is to increase cost efficiency. The goal of this study is to quantify the level of persistent and transient cost efficiency of individual firms by applying the generalized true random effects (GTRE) model introduced by Colombi, Kumbhakar et al. (2014a) and Filippini and Greene (2016). Applying this newly developed GTRE model to a total cost function, the level of cost efficiency of 65 Swiss hydropower firms is analyzed for the period between 2000 and 2013. A true random effects specification is estimated as a benchmark for the transient level of cost efficiency. The results show the presence of both transient as well as persistent cost inefficiencies. The GTREM predicts the aggregate level of cost inefficiency to amount to 22.3 percent (7.9 percent transient, 14.4 percent persistent) on average between 2000 and 2013. These two components differ in interpretation and implication. From an individual firm's perspective, the two types of cost inefficiencies might require a firm's management to respond with different improvement strategies. The existing level of persistent inefficiency could prevent the hydropower firms from adjusting their production processes to new market environments. From a regulatory point of view, the results of this study could be used in the scope and determination of the amount of financial support given to struggling firms.

**Keywords:** Efficiency measurement, stochastic frontier analysis, persistent and transient cost efficiency, hydropower

**JEL classification:** C01, C23, D23, L94, Q25

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## Acknowledgment

We are grateful to the Bundesamt für Energie (BFE) for financially supporting a large study on the cost structure of the Swiss hydro power firms. The content of this paper does not necessarily represent the official views of BFE. All omissions and remaining errors are our responsibility. Furthermore, we would like to thank Nilkanth Kumar and the participants of the Mannheim Energy Conference 2015 and the 14th European Workshop on Efficiency and Productivity Analysis for their helpful comments.

# 1 Introduction

Ever since Switzerland's electrification at the beginning of the 20<sup>th</sup> century, hydropower has been the country's main domestic source of electricity. Over time, Swiss hydropower firms have consolidated their position as reliable, cost effective and renewable base and peak load electricity producers. Hydropower also has enabled Switzerland to play an active role on the European electricity market. The pursued business models can roughly be summarized as follows: run-of-river plants produce base load electricity while storage and pump-storage plants use their natural water inflows to help covering electricity demand at peak hours, usually occurring at noon and early evening. All three technology types not only produce for the domestic market, but also are extensively involved in exporting activities to the European grid. A special role is accorded to the pump-storage plants, whose business model exploits the spread between peak and off-peak electricity prices. In addition of using natural water inflows for electricity generation, they pump water into their reservoirs during off-peak hours at favorable prices—often during nighttime—by consuming electricity directly from the high voltage grid. This electricity is partly sourced from the European electricity market, and especially from the French nuclear fleet. At peak load times, the water is turbinated again and the generated electricity is sold at comparatively high prices.

This business model was very successful until 2008. Then, the economic crisis, the low price of coal, the low price of CO<sub>2</sub> certificates not reflecting the emission's external costs and the subsidy system for renewable energies such as wind and photovoltaics have led to a significant drop in overall market prices for electricity. In addition, the

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spread between peak and off-peak electricity prices on the European electricity markets have decreased or at some hours even completely disappeared. In this context, the competitiveness of the coal power plants has increased significantly. Furthermore, since 2009 the Swiss electricity market has been partially liberalized, giving electricity distribution companies and large customers consuming more than 100 MWh per year the possibility to purchase electricity from a producer of their choice in Switzerland or other European countries or to buy electricity directly on the European spot markets. Of course, this reform has increased the level of competition among the Swiss hydropower firms resulting in a pressure to reduce production costs. In January 2015, the decoupling of the Swiss Franc from the Euro has led to an additional reduction in margins, since the electricity traded on a European level is denominated in Euros. For these reasons, a growing share of hydropower plants has started to incur financial losses in recent years. In the current competitive context, it is of immediate importance for them to identify strategies to increase competitiveness by reducing production costs.

One possibility to achieve such goal is to improve the level of cost efficiency, which, as discussed in Colombi, Kumbhakar et al. (2014a) and Filippini and Greene (2016), can be split into two parts: a persistent and a transient one. The persistent part captures cost inefficiencies which do not vary with time. These could be inefficiencies due to recurring identical management mistakes, structural problems within the electricity generation process or factor misallocations that are difficult to change over time. On the other hand, the transient component represents cost inefficiencies varying with time, e.g., singular, non-systematic management mistakes. In the short- to medium-run, a firm's leverage is expected to be mainly on the improvement of the transient part of cost efficiency.

Information on the level of cost efficiency is of importance not only for the firms, but also for the Swiss federal government. In fact, in 2015 the Swiss parliament decided, under some circumstances, to financially support hydropower firms in financial distress. However, the political process of specifying the details of such a subsidization system is still ongoing. From an economic policy point of view, it is important to grant such subsidies only to firms operating already with a high degree of efficiency. Hence, knowledge on the level of cost efficiency supports the government in avoiding subsidizing inefficient hydropower firms.

Despite the fact that hydropower still is the world's dominant source of renewable energy, the scientific literature only comprises a few published studies on the productive efficiency of hydropower firms.<sup>2</sup> Banfi and Filippini (2010) study the cost structure and level of cost efficiency of an unbalanced panel of 43 Swiss hydropower firms observed from 1995 to 2002. Using a translog variable cost function, they employ the true random effects model proposed by Greene (2005a, b), i.e. a stochastic frontier approach. The explanatory variables considered are: total amount of electricity produced, number of plants per firm, price of labor and capital stock. Furthermore, four binary in-

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<sup>2</sup> For a publication summarizing several studies on efficiency measurement in the general electricity generation sector see, e.g., Barros (2008). More recent contributions to the measurement of efficiency in the electricity generation sector were made, e.g., by Yang and Pollitt (2009) (China – coal plants – DEA), Sueyoshi, Goto et al. (2010) (USA – coal plants – DEA), Liu, Lin et al. (2010) (Taiwan – thermal plants – DEA), Shrivastava, Sharma et al. (2012) (India – coal plants – DEA), See and Coelli (2012) (Malaysia – thermal plants – SFA) and Chen, Barros et al. (2015) (China – thermal plants – Bayesian SFA).

dicators are added to the model controlling for different types of technology.<sup>3</sup> Their empirical results indicate economies of utilization as well as the presence of cost inefficiency. By also using a variable cost function approach, Barros and Peypoch (2007) examine the cost efficiency of a balanced panel of 25 Portuguese hydropower plants, all of them belonging to the main Portuguese utility, for the years 1994 to 2004.<sup>4</sup> From the econometric point of view, these authors also use a translog functional form and the true random effects model. Finally, Barros, Chen et al. (2013) analyze the level of cost efficiency of a relatively small panel of twelve Chinese hydropower firms for the period 2000 to 2010 using a total cost function in translog functional form. They use a stochastic frontier latent class model to take into account possible differences in the unobserved production technology affecting costs. The estimation results obtained indicate the presence of three distinct groups of firms. Their choice to use a latent class model is an interesting approach for the case where the firms' production technology is not directly observed.

Most of the empirical literature so far has fallen short of a differentiation of the persistent and transient component of productive efficiency. Also the aforementioned studies provide only empirical information on the transient, but not the persistent, part of cost efficiency. This paper's main goal therefore is to measure the level of persistent and transient cost efficiency for a sample of Swiss hydropower firms by estimating a

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<sup>3</sup> The cost function specified in Banfi and Filippini (2010) was also used by Filippini and Luchsinger (2007) to quantify the economies of scale of the Swiss hydropower sector using cost share equations and the seemingly unrelated regression concept of Zellner (1962).

<sup>4</sup> Using the same data and looking at the years 2001 to 2004, Barros (2008) analyzes and decomposes the productivity of the hydropower firm by using data envelopment analysis (DEA) applied to a production function.

homothetic translog frontier total cost function. We use a new and representative panel of Swiss hydropower firms. In a firm's context, the persistent part of productive inefficiency may be due a variety of factors like regulations, investments in inefficient machines or infrastructure or lasting habits of the management to waste inputs. The transient part of inefficiency on the other hand, for example, may stem from temporal behavioral aspects of the management or from a non-optimal use of some machines. Such distinction and measurement of the two components of overall cost efficiency is interesting because it allows the firms to elicit their cost saving potential in the short- as well as the long-run. Also, from a policy point of view, firms can be asked to improve their cost efficiency if they, e.g., become part of a subsidization program, as it is currently being discussed in Switzerland. Within the framework of such a program, the policy maker can ask the participating firms to improve their level of cost efficiency. Thereby, he should differentiate between persistent and transient levels of efficiency.

The contribution of this paper to the scientific literature is threefold. Firstly, from an econometric point of view, we provide the first stand-alone empirical application of a novel approach recently introduced by Filippini and Greene (2016). Their methodology allows for a splitting of the level of productive efficiency into a transient and a persistent part. Secondly, a rich cost model specification is used, explicitly controlling, e.g., for the technological heterogeneity between run-of-river, storage and pump-storage plants. Thirdly, firm-level information on the two categories of persistent and transient cost inefficiency can help the government to design an effective subsidy policy by granting financial aids only if the firms meet predefined efficiency standards in both categories.

The structure of this paper is as follows: Section 2 contains a description and gives an overview of the data used for the empirical analysis. Section 3 describes the empirical cost model as well as the chosen functional form, and section 4 presents the econometric estimation methodologies. Results are summarized in section 5. Finally, section 6 concludes and discusses the findings.

## 2 Data

Hydropower electricity generation in Switzerland is mainly based on approximately 600 plants operated by several dozen hydropower firms<sup>5</sup>, contributing roughly 55 to 60 percent to the total domestic electricity generation. Most of these plants (ca. 80 percent) are of run-of-river type, with storage and pump storage plants making up the remaining share (BFE, 2013). The Swiss hydropower firms are organized according to a specific structure, with the largest part of them being so-called partner firms (“Partnerwerke”). These firms sell the generated electricity to Swiss utilities who in turn are mainly active in the distribution, sales and trading of electricity in Switzerland as well as on the European electricity market.

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<sup>5</sup> A hydropower firm may have several plants under operation. A plant represents a building containing one or more turbines. Geographically, these plants usually are located in a close perimeter to each other.

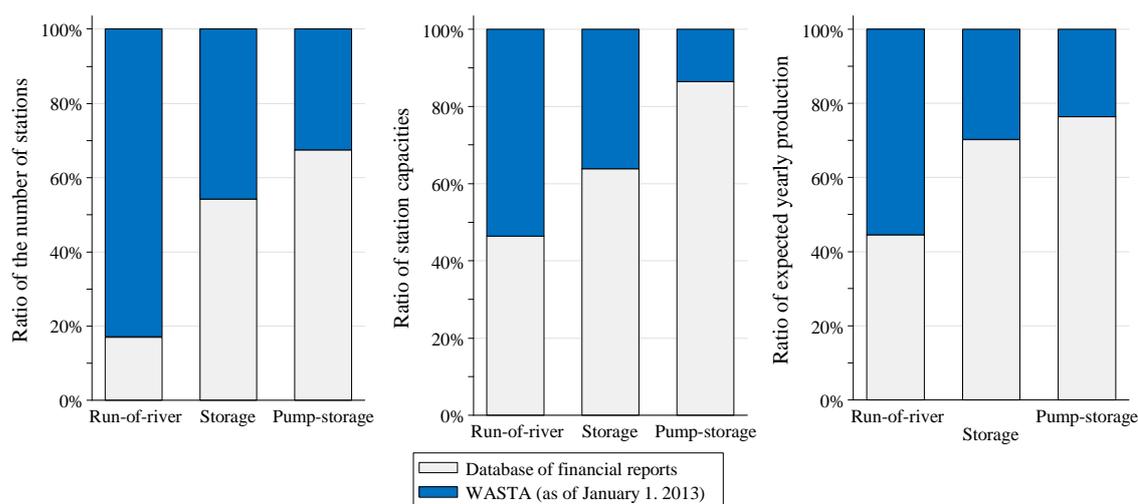
The econometric analysis is based on an unbalanced<sup>6</sup> panel data set comprising 65 hydropower firms over the time period of 2000 to 2013. Most of these firms are “Partnerwerke”. The financial data was extracted from the yearly annual reports of these firms and extended by firm specific technical information contained in the “Statistik der Wasserkraftanlagen der Schweiz” (WASTA), which is published annually by the Swiss Federal Office of Energy (BFE, 2013). By means of this technical information, hydropower firms are classified into three distinctive categories to account for heterogeneities in the production processes of the power plants. The three categories, representing the dominating power plant type operated by a firm, are: run-of-river, storage and pump storage. Following Filippini, Banfi et al. (2001), the classification is conducted as follows: Storage power firm produce at least 50 percent of their expected electricity generation by storage power plants, whereby the share of the installed pump capacity is smaller or equal to 10 percent of the total maximum possible generator capacity. A pump storage power firm produces at least 50 percent of its expected electricity generation by storage power plants, whereby the share of the installed pump capacity is larger than 10 percent of the total maximum possible generator capacity. All other firms are considered to be of type run-of-river.

A specific firm type does not imply all plants operated by this firm being of same kind; it rather indicates the dominating plant type. The plant types of the firms classified to be of type run-of-river are relatively homogenous, i.e. most of these firms exclusively or to a large extent operate run-of-river plants. Furthermore, this firm type

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<sup>6</sup> The underlying reasons for the data to be unbalanced are, for example, firm mergers or annual reports not being obtainable anymore due to, e.g., ownership changes. None of the sample attrition was due to firms ceasing production.

runs comparatively few plants, usually one or two. This is in contrast to the plants run by the storage and pump storage firms, which are more diverse in type and larger in number per firm. The average share of run-of-river type firms in our sample is 58 percent. The share of storage type firms is 19.9 and 22.1 percent for pump storage type firms. Our sample of hydropower firms represents the Swiss hydropower sector quite well, especially in terms of the installed capacity and expected generation (cf. Figure 1). For the period 2000 to 2013, we observe approximately 60 percent of the total expected generation of the Swiss hydropower plants with an installed capacity larger than 300 kW.



**Figure 1:** Representativeness of the sample in terms of the number of stations, the installed capacity and the expected generation in 2013.

*Note:* Figure 1 shows the degree, to which firms of the sample are representative of the population of Swiss hydropower stations with an installed capacity of at least 300 kW. This population of stations is contained in the WASTA. For example, the right bar of the right panel indicates our sample to represent roughly 80 percent of the expected yearly generation of the population of pump-storage plants.

The power plants usually are not older than 50 years or have undergone at least once a major remodeling during the last five decades. The highest share of plants in our

sample is located in Alpine cantons, which corresponds to the general distribution of hydropower plants in Switzerland. For topological and hydrological reasons the storage and pump-storage firms are mainly situated in the Alpine cantons.

## 3 Empirical Specification

### 3.1 Parametrization of the Cost Function

The frontier total cost function represents the minimum cost a firm potentially could achieve in producing a given amount of output by using a given technology and facing given input prices. Usually, none or only a few firms are operating at the cost frontier. Failure to do so implies the existence of technical and allocative inefficiency. In what follows, a stochastic frontier total cost function is estimated using panel data. Such estimation of the frontier necessitates the specification of a parametric model, the choice of a functional form and finally, the identification of an econometric approach.

The cost of a firm operating one or more hydropower plants is influenced by several factors such as output, factor prices, size of the reservoir, production technology (storage, pump-storage or run-of-river), age or the number of hydropower plants in a firm's portfolio. Therefore, the cost function for the Swiss hydropower firms may be specified as

$$C = c(Y, P_L, P_W, P_K, P_E, F, N, D_S, D_P, t), \quad (1)$$

where  $C$  are the total generation costs. Firm  $i$  and time  $t$  subscripts are dropped for notational simplicity. The single output,  $Y$ , is gross electricity generation in kWh. The price of labor is represented by  $P_L$ , the price of water by  $P_W$  and the residual price of capital by  $P_K$ . The price of energy used in electricity production is  $P_E$ . To capture additional heterogeneities in the production process, the cost function includes on the one hand the firm's average load factor  $F$ . This variable helps to differentiate between, e.g., a run-of-river or storage firm, as the latter usually shows a much lower load factor than the former.<sup>7</sup> To further control for the presence of different types of hydropower firms, technology fixed effects  $D_S$  and  $D_P$  are included into the model. These indicate whether a firm uses predominantly storage ( $D_S$ ) or pump-storage ( $D_P$ ) plants for electricity generation, with run-of-river representing the reference firm type.<sup>8</sup> With run-of-river firms bunching up in the Swiss midlands, and storage and pump storage firms being concentrated in Alpine regions, these variables in addition capture heterogeneity in terms of the production environment. Finally, the number of plants under operation,  $N$ , measures the

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<sup>7</sup> Next to being inherently connected to a power plant's technology, a low load factor also could indicate unplanned plant shutdowns due to, e.g., poor maintenance of machinery. A subsequent repair would result in higher costs, translating into a poorer productive efficiency. However, the annual reports indicate that shutdowns either were occurring for planned maintenance or due to adverse natural conditions. Furthermore, firms in general avoid water overflows as marginal generation costs usually are low. Therefore, and given the data's yearly aggregation and the extent of the installed capacity being defined by long-term investment cycles, the load factor can be considered to be exogenous.

<sup>8</sup> Another approach to capture heterogeneities in the production process would consist of an application of a latent class model, as done in, e.g., Barros et. al. (2013). However, we decided against this approach, because we observe technological heterogeneity. We are also more interested in the distinction between persistent and transient inefficiency. We believe that the latent class model is not completely appropriate for the estimation of a cost function based on a small sample and that our cost model specification and econometric approach sufficiently controls for heterogeneities in the production processes.

impact on cost of jointly operating several plants. Even though electricity generation by hydropower is based on mature technologies, a time trend  $t$  is included to capture exogenous technological change. Total costs are based on an accounting approach. Hence, it is worth noting that the framing of the cost function follows a firm oriented perspective rather than a society oriented one, i.e. the cost function does not account for possible external costs arising from the electricity generation process.

Under the assumption of cost minimizing firms, a cost function should satisfy the properties of concavity and linear homogeneity in input prices. Furthermore, it should be non-decreasing in output and input prices. Linear homogeneity in input prices can be imposed by normalizing cost and input prices by one of the input prices. The other properties are to be verified once the translog cost function has been estimated. We justify the necessary assumption of output levels being exogenous to hold based on the monopolistic structure of the electricity market. Firms faced public service obligations for most of the years considered in the empirical analysis. Furthermore, the majority of firms contained by the sample are so called partner firms (“Partnerwerke” in German). A shareholder (usually one or several utilities that trade and sale electricity, also called mother companies) of a partner firm has the right to claim a percentage share of the electricity produced depending on the share of paid in capital. Utilities then use this electricity to partially cover domestic electricity demand as well as for export activities. The general production plan of this firm type is defined on an annual basis, instead of a daily basis depending on market conditions.

We decided to use a translog functional form (Berndt and Christensen, 1973; Christensen, Jorgenson et al., 1973) to estimate the cost function in eq. (1). In a prelimi-

nary analysis, we tried to estimate a fully flexible version of the translog functional form. However, due to the presence of highly correlated variables in the cost model, such as output, load factor or number of stations, such model specification suffered from multicollinearity. For this reason, we decided to estimate a homothetic version of the translog cost function, a version that is more parsimonious in the number of coefficients to be estimated. Based on eq. (1) the homothetic version of the translog cost function can be expressed as shown in eq. (2).

$$\begin{aligned}
c = & \alpha + \beta_y y + \sum_{x=\{l,w,k\}} \beta_x p_x + \sum_{z=\{F,n\}} \beta_z z \\
& + \frac{1}{2} \left( \beta_{yy} y^2 + \sum_{x=\{l,w,k\}} \beta_{xx} p_x^2 + \sum_{z=\{F,n\}} \beta_{zz} z^2 \right) + \sum_{x=\{w,k\}} \beta_{lx} p_l p_x + \beta_{wk} p_w p_k \quad (2) \\
& + \sum_{z=\{F,n\}} \beta_{yz} yz + \beta_{Fn} Fn + \beta_{DS} D_S + \beta_{DP} D_P + \beta_t t + u + v.
\end{aligned}$$

For notational simplicity, the unit index  $i$  as well as the time index  $t$  are omitted. Lower cases indicate values in natural logarithms, and  $\alpha$  is the intercept. Linear homogeneity in prices is imposed by normalizing total costs and factor price variables by the price of energy. Because of its comparative robustness with regard to outliers, the variables' median value was chosen as point of approximation, i.e. the estimated coefficients represent elasticities at the sample's respective median values. As will be explained in section 4, the concept of the stochastic frontier analysis splits the error term  $\varepsilon$  into an inefficiency component  $u$  and the usual white noise term  $v$ , i.e.  $\varepsilon = u + v$ .

## 3.2 Variable Definitions

Total generation costs include water fees, amortization, financial expenses, profit before taxes, material and external services, personnel costs, costs for energy and grid access, other taxes and dues as well as other costs. All financial variables have been deflated to real 2010 values using the Swiss producer price index published by BFS (2014). The price of labor,  $P_L$ , is defined as personnel costs divided by the number of employees. For firms with missing information on the price of labor, a year and region specific price proxy is constructed, thereby allowing for structural differences in salaries between geographic regions.<sup>9</sup> The price of water,  $P_W$ , is defined as the ratio of the sum of water fees and other concession fees to a firm's total installed turbine capacity. Following (Friedlaender and Wang Chiang, 1983), the capital price,  $P_K$ , is estimated as residual costs divided by the installed turbine capacity, which serves as a proxy for the capital stock. Residual costs are defined as total costs minus labour costs, energy costs and water costs, i.e. they include material and external service costs, allowances for depreciation, financial expenses and profits before taxes<sup>10</sup>. Finally, a single energy price,  $P_E$ , is assumed for all hydropower firms. In fact, energy costs are mainly composed of expenditures on electricity. The presence of a uniform European electricity market justifies the assumption of firms facing a cross-section wise constant price of electricity.

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<sup>9</sup> This labor price proxy represents the year specific median labor price in a region. The seven geographic regions of Switzerland are defined as follows: Lake Geneva region (1), midland (2), Northwestern Switzerland (3), Zurich (4), Eastern Switzerland (5), Central Switzerland (6), Ticino (7). Furthermore, for the firms located on the German and French border, two separate regions (8 and 9) are defined.

<sup>10</sup> Profits before taxes are assumed to represent the equity yield rate. Unfortunately, we do not have all the information necessary to estimate a capital price based on the economic approach of opportunity costs of capital.

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Some firms activated additional capital allowances on non-depreciable investments before the opening of the electricity market to increase the level of competitiveness, especially around the beginning of the new millennium. As some of these additional allowances exceed usually observed numbers by a multiple, they cause a significant distortion of the respective firms' cost structure. To avoid the distorting effect of such special accounting measures, extraordinary allowances in one year were corrected for by adjusting the amortization rate of that year to the firm specific average amortization rate of the other years.<sup>11</sup> Furthermore, if mother companies delivered pump energy free of charge, these opportunity costs were valued and subsequently added to total costs.<sup>12</sup> Finally, the load factor  $F$  is formed by a division of  $Y$ , the gross electricity generation, by the total installed turbine capacity, whereby the latter is multiplied by the number of hours per year. The variables' descriptive statistics are given in Table 1.

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<sup>11</sup> Such amortization cost correction affected 8 firms in a total of 14 periods, i.e. ca. 1.7 percent of the observations. The amortization rate is the ratio of the amortization costs to the sum of the reported book value of fixed assets (excluding assets under construction) and realized investments. We chose the book value because not all hydropower firms publish numbers on asset acquisitions. However, the use of the book value implies a non-linear depreciation schedule, while hydropower firms usually depreciate linearly.

<sup>12</sup> This correction only affects 5 firms in a total of 39 periods, i.e. ca. 4.5 percent of the observations. The correction for non-allocated pump energy charges at a rate of 3 cents per kWh accounts for the fact that consumed pump energy is of different quality than the electricity generated by a pump storage plant: From 2000 to 2013 (our sample period), water usually was pumped at nighttime when electricity prices were low. Electricity generation, however, focused on peak load times, usually at noon and in the evening, since these periods were characterized by high prices.

*Table 1: Descriptive statistics of the variables.*

|  | Mean   | Std.dev. | Min.  | Max.    |
|--|--------|----------|-------|---------|
| Total costs $C$ [million CHF]            | 24.20  | 30.96    | 0.32  | 195.92  |
| Electricity generation $Y$ [GWh]         | 433.38 | 484.06   | 5.82  | 2695.00 |
| Price of labor $P_L$ [kCHF per employee] | 127.80 | 19.10    | 74.90 | 247.15  |
| Price of water $P_W$ [CHF per kW]        | 45.41  | 34.64    | 0.54  | 336.98  |
| Price of capital $P_K$ [CHF per kW]      | 145.90 | 108.22   | 17.00 | 739.68  |
| Load Factor $F$ [index]                  | 0.492  | 0.331    | 0.104 | 2.608   |
| Number of stations $N$                   | 2.49   | 2.03     | 1     | 13      |
| Time trend $t$                           | 7.46   | 4.02     | 1     | 14      |
| Storage fixed effect $D_S$               | 0.199  | 0.400    | 0     | 1       |
| Pump storage fixed effect $D_P$          | 0.221  | 0.415    | 0     | 1       |

*Note:* This table presents descriptive statistics of the variables of the cost function given in eq. (1). CHF indicates Swiss Francs. The statistics are based on the full sample of observations. Monetary values are given in real 2010 values.

## 4 Estimation Methodologies

In what follows, the level of cost efficiency of a sample of Swiss hydropower firms is estimated using a parametric approach, i.e. the stochastic frontier analysis (SFA).<sup>13</sup> Econometric SFA models for panel data allow both the estimation of the transient and persistent part of the cost inefficiency. Moreover, parametric approaches are suitable in

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<sup>13</sup> The literature on the measurement of a firm's productive efficiency roughly can be divided into two main methodological strands: the parametric and the non-parametric analysis. SFA represents the prevalent parametric approach, whereas the data envelopment analysis (DEA) constitutes the most prominent non-parametric approach. Non-parametric approaches do not necessitate an a priori specification of a functional form and use linear programming, while parametric approaches are based on econometric concepts, allowing them to differentiate between unobserved heterogeneity and inefficiency. Furthermore, non-parametric approaches are not able to distinguish in a satisfactory way between technical and allocative cost inefficiency, which together form the overall cost inefficiency.

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cases of unobserved heterogeneity influencing production processes, like environmental characteristics.<sup>14</sup>

The measurement of inefficiency using SFA has a long-standing tradition in the literature. The SFA methodology dates back to the end of the 1970s when first contributions—at that time focusing exclusively on cross-sectional data—were made by Aigner, Lovell et al. (1977), Meeusen and Broeck (1977) and Battese and Corra (1977). Since then, the concept of SFA was extended significantly to the longitudinal setting by Pitt and Lee (1981), Cornwell, Schmidt et al. (1990) and Greene (2005).<sup>15</sup> Recently, Colombi, Martini et al. (2011) have proposed a new stochastic frontier model that simultaneously distinguishes between two parts of productive efficiency, i.e. a persistent and a transient part. However, estimation of this model resulted to be complex and cumbersome. Subsequently, Tsionas and Kumbhakar (2014), Kumbhakar, Lien et al. (2014) and Filippini and Greene (2016) proposed different econometric approaches to estimate the model proposed by Colombi, Martini et al. (2011).

In this paper, we decided to use two alternative stochastic frontier models for panel data. The first is the true random effects model (TREM hereafter) proposed by Greene (2005a, 2005b) that produces values of the productive inefficiency that vary over time (transient inefficiency). The TREM includes group-specific random effects to capture any time-invariant unobserved heterogeneity. Further, as in the basic stochastic frontier model proposed by Aigner, Lovell et al. (1977), the error term is composed of

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<sup>14</sup> A more extensive discussion on methodological differences as well as an extensive description of SFA models can be found in, e.g., Greene (2008), Coelli, Rao et al. (2005) or Kumbhakar and Lovell (2000).

<sup>15</sup> See Filippini and Greene (2015) for a review of several stochastic frontier models for panel data.

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two parts: a stochastic error capturing the effect of noise and a one-sided non-negative disturbance representing the level of inefficiency. The TREM has the advantage to control for time-constant unobserved heterogeneity. On the other side, any time-invariant component of inefficiency is absorbed in the group-specific random effects. Therefore, the TREM tends to produce an estimate of the level of transient inefficiency.

The second econometric model is the generalized true random effects model (GTREM). This model offers the possibility to estimate at the same time the transient as well the persistent component of the productive inefficiency. As discussed previously, Colombi, Kumbhakar et al. (2014b) have provided a first theoretical and empirical discussion on the distinction between persistent and transient inefficiency. For this purpose, they specify a four random components model. By recognizing that the sum of the four random components has a closed skew-normal distribution, they apply a maximum likelihood estimation for the numerical optimization, which in practice however is highly complex and cumbersome to estimate. The coefficients are estimated using the two step procedure of Parke (1986), which gives unbiased estimates of the  $\beta$ -coefficients (except the intercept) in a first step and of the variances of the four random components as well as the intercept in a second step. In a final third step, the four components' posterior expected values are calculated by using the respective closed-form conditional likelihood functions.

To measure transient and persistent efficiency, Tsionas and Kumbhakar (2014) propose the estimation of a four-way error component model based on Bayesian Markov chain Monte Carlo methods. Kumbhakar, Lien et al. (2014) introduce a method of moments estimator based on OLS to simultaneously estimate persistent and transient in-

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efficiency and test this estimator against five other panel data models. Colombi, Kumbhakar et al. (2014a), however, find their approach to yield more efficient and less biased estimation results than the one in Kumbhakar, Lien et al. (2014). They also test their model against several other standard SFA models and find the four-way error component model—due to its ability to distinguish between unobserved latent heterogeneity and persistent inefficiency—to be appropriate especially if the panel is moderately long and characterized by a relatively high degree of firm heterogeneity.

Building on the theoretical platform provided by Colombi, Kumbhakar et al. (2014a), Filippini and Greene (2016) suggest a practical, straightforward and transparent econometric method to estimate the GTREM. Filippini and Greene (2016) propose to estimate the two components of productive efficiency using a full information maximum simulated likelihood estimator. The highly complicated log likelihood function noted in Colombi, Kumbhakar et al. (2014a) is simplified by exploiting the formulation of Butler and Moffitt (1982) in the simulation, where the log-likelihood function is computed using Hermite quadrature. The log-likelihood function then is estimated by maximum simulated likelihood using Halton sequences. Instead of using four unique disturbance terms as in Colombi et. al. (2014), Filippini and Greene (2016) propose to define a two-part disturbance term. Each part of the disturbance term is characterized by a skewed normal distribution with, in each case, one part assumed to be time-invariant and the other to be time-variant. The only difference between the TREM and GTREM setting therefore consists of the latter model containing a skewed normally instead of normally distributed time invariant disturbance term.

The firm's level of efficiency for the TREM is estimated using the conditional mean of the inefficiency term proposed by Jondrow et al. (1982). The firm's efficiency for the GTREM is estimated using the expression presented in Filippini and Greene (2015). Table 2 summarizes the econometric specification of the two models.

**Table 2:** *Distributional assumptions of the stochastic cost frontier models.*

|                                      | TREM                                    | GTREM   |
|--------------------------------------|---|---|
| Full random error $\varepsilon_{it}$ | $\varepsilon_{it} = r_i + u_i + v_{it}$ | $\varepsilon_{it} = r_i + h_i + u_i + v_{it}$ |
|                                      | $u_{it} \sim N^+(0, \sigma_u^2)$        | $u_{it} \sim N^+(0, \sigma_u^2)$              |
|                                      | $v_{it} \sim N(0, \sigma_v^2)$          | $v_{it} \sim N(0, \sigma_v^2)$                |
|                                      | $r_i \sim N(0, \sigma_r^2)$             | $r_i \sim N(0, \sigma_r^2)$                   |
|                                      |   | $h_i \sim N^+(0, \sigma_h^2)$                 |
| Persistent inefficiency estimator    | None                                    | $E[h_i   \varepsilon_{it}]$                   |
| Transient inefficiency estimator     | $E[u_{it}   \varepsilon_{it}]$          | $E[u_{it}   \varepsilon_{it}]$                |

*Note:* This table presents the distributional assumptions of the stochastic error and inefficiency components of the TREM and GTREM stochastic frontier models.

## 5 Results

### 5.1 Cost Function Parameters

The estimated coefficients of the two frontier models as well as their respective standard errors are listed in Table 3. Linear homogeneity was imposed a priori by normalizing prices and output with respect to the constant electricity price. To ensure monotonicity, microeconomic theory demands the cost function to be increasing in generated electricity and input prices. Furthermore, the function is expected to be concave with respect to

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input prices. Such concavity implies own-price elasticities being negative with the Hessian matrix of second order partial derivatives of total costs with respect to prices being negative semi-definite.<sup>16</sup> The cost function is generally well behaved; except for the concavity condition (one of the four eigenvalue is greater than zero), our results obey these restrictions (cf. Table 8 and Table 9 in the appendix). We justify the slight violation of the concavity condition by the estimation of a behavioral cost function: the frontier cost model builds on the implicit assumption of firms not fully minimizing costs, which contradicts the concavity condition's underlying assumption of cost minimizing firms.<sup>17</sup>

The estimated coefficients in general have the expected sign and many are, together with  $\lambda$ <sup>18</sup>, statistically significant at a level of 1 percent. The magnitude of the estimated coefficients is similar across both models. Technological progress in the hydropower sector is small; major technological components like turbines or dams can be considered as comparatively mature. Therefore, the negative coefficient estimate of the neutral, exogenous and progressive technical change  $t$  is not surprising.<sup>19</sup>

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<sup>16</sup> See the appendix for a detailed description of the properties.

<sup>17</sup> See Bös (1989) for a discussion on behavioral cost functions.

<sup>18</sup> Lambda ( $\lambda$ ) expresses the ratio of the standard deviation of the inefficiency term  $u_{it}$  to the standard deviation of the stochastic term  $v_{it}$ .

<sup>19</sup> Filippini and Luchsinger (2007) find a significant effect of technical change in the Swiss hydropower sector of -0.018. They estimate a translog variable cost model using seemingly unrelated regression and an unbalanced sample of 43 firms for the period of 1995 to 2002. In Banfi and Filippini (2010), statistically significant technical change amounts to -0.025. They estimate a translog variable cost function applying a TREM specification and use the same data as Filippini and Luchsinger (2007).

**Table 3:** Cost function estimation results of the TREM and GTREM specification.

|                                      | TREM      |          | GTREM     |          |
|--------------------------------------|-----------|----------|-----------|----------|
|                                      | Coef.     | Std.dev. | Coef.     | Std.dev. |
| Electricity generation ( $\beta_y$ ) | 0.500***  | (0.006)  | 0.486***  | (0.006)  |
| Labor price ( $\beta_l$ )            | 0.058***  | (0.016)  | 0.082***  | (0.017)  |
| Water price ( $\beta_w$ )            | 0.171***  | (0.005)  | 0.161***  | (0.005)  |
| Residual capital price ( $\beta_k$ ) | 0.629***  | (0.003)  | 0.654***  | (0.003)  |
| Number of stations ( $\beta_n$ )     | 0.309***  | (0.009)  | 0.368***  | (0.010)  |
| Load factor ( $\beta_F$ )            | -0.657*** | (0.009)  | -0.615*** | (0.008)  |
| Time trend ( $\beta_t$ )             | -0.162    | (0.003)  | -0.140**  | (0.003)  |
| ( $\beta_{yy}$ )                     | 0.280***  | (0.095)  | 0.114***  | (0.106)  |
| ( $\beta_{ll}$ )                     | 0.057***  | (0.004)  | 0.055     | (0.004)  |
| ( $\beta_{ww}$ )                     | 0.212***  | (0.009)  | 0.176***  | (0.008)  |
| ( $\beta_{kk}$ )                     | 0.297***  | (0.014)  | 0.421***  | (0.015)  |
| ( $\beta_{nn}$ )                     | 0.084***  | (0.003)  | 0.074***  | (0.003)  |
| ( $\beta_{FF}$ )                     | 0.052***  | (0.022)  | 0.054***  | (0.020)  |
| ( $\beta_{tw}$ )                     | -0.065**  | (0.021)  | -0.030*** | (0.025)  |
| ( $\beta_{lk}$ )                     | -0.056*** | (0.006)  | -0.043    | (0.005)  |
| ( $\beta_{wk}$ )                     | 0.024***  | (0.005)  | -0.027*** | (0.005)  |
| ( $\beta_{yn}$ )                     | 0.197***  | (0.003)  | 0.188***  | (0.003)  |
| ( $\beta_{yF}$ )                     | -0.141*** | (0.007)  | -0.149*** | (0.007)  |
| ( $\beta_{nF}$ )                     | 0.263***  | (0.007)  | 0.179***  | (0.006)  |
| Storage FE ( $\beta_{DS}$ )          | 0.421***  | (0.008)  | 0.815***  | (0.011)  |
| Pump storage FE ( $\beta_{DS}$ )     | 0.001***  | (0.000)  | 0.001***  | (0.000)  |
| Constant ( $\alpha_0$ )              | 16.895*** | (0.010)  | 16.650*** | (0.011)  |
| Number of observations               | 873       |          | 873       |          |
| Unit specific constant ( $r_i$ )     | 0.188***  | (0.002)  | 0.221***  | (0.003)  |
| $\lambda$                            | 3.564***  | (0.310)  | 4.195***  | (0.406)  |
| $\sigma$                             | 0.092***  | (0.002)  |           |          |
| $\sigma_r$                           |           |          | 0.096***  | (0.002)  |
| $\sigma_h$                           |           |          | 0.816***  | (0.030)  |
| Log Likelihood                       | 1099.57   |          | 1084.05   |          |

*Note:* This table presents the estimation results when applying the TREM and GTREM to the total cost function given in eq. (2). *FE* abbreviates “fixed effect”. Robust standard errors at the firm level are reported in parenthesis. Asterisks \*\*\* indicate significance at 1 percent level, \*\* at 5 percent level and \* at 10 percent level.

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The first order coefficients of the translog function are interpretable as elasticities at the sample median with the constant representing the total costs at the approximation point. The elasticity of the generated electricity is positive and highly statistically significant. The negative and statistically significant load factor indicates higher total costs for storage and pump storage firms compared to their run-of-river counterparts, since the former technologies generally are characterized by comparatively low load factors. The firm-types fixed effects also point towards higher costs of storage and especially pump storage firms. Examples of factors contributing to these higher costs could be, next to the pump energy consumption of the latter type, relatively high investment costs for storage technologies in general, a higher complexity of operating such plants as well as their geographical remoteness.

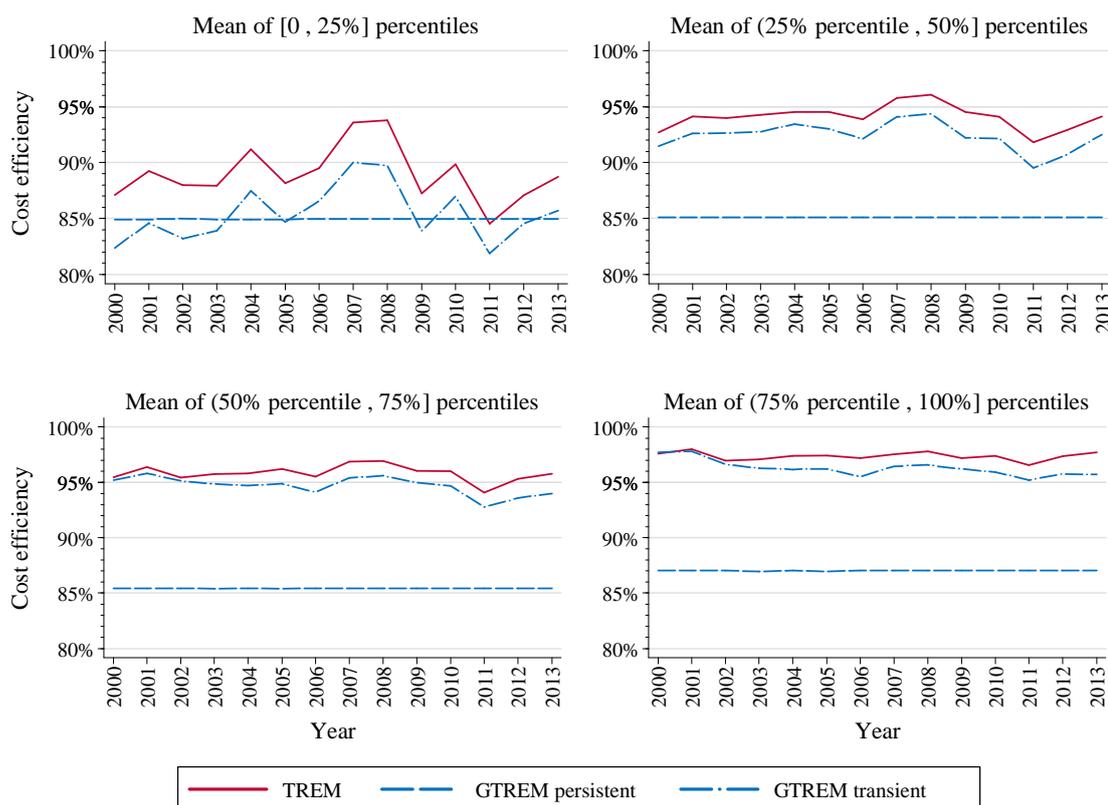
## 5.2 Cost Efficiency

Table 4 provides descriptive statistics of the estimated levels of cost efficiency. The median transient efficiency of the TREM of 95.1 percent is relatively similar in magnitude to the median transient result of the GTREM of 93.9 percent. The dispersion of the estimated transient efficiencies is slightly higher for the TREM than for the GTREM. As depicted by Figure 2, mean efficiency estimates within the four quartiles of the yearly efficiency distributions are relatively constant across time, independently of the model specification. Hence, we find robust empirical evidence that Swiss hydro power firms on average neither strongly increased nor decreased their transient as well as persistent cost efficiency between 2000 and 2013.

**Table 4:** Descriptive statistics of estimated cost efficiencies.

|          | GTREM<br>persistent | TREM  | GTREM<br>transient |
|----------|---------------------|-------|--------------------|
| Mean     | 0.856               | 0.940 | 0.921              |
| Min      | 0.844               | 0.705 | 0.670              |
| Max      | 0.897               | 0.993 | 0.992              |
| Std.dev. | 0.011               | 0.041 | 0.051              |
| 25% Pc.  | 0.851               | 0.928 | 0.907              |
| Median   | 0.852               | 0.951 | 0.939              |
| 75% Pc.  | 0.857               | 0.967 | 0.954              |

*Note:* This table presents descriptive statistics of the cost efficiency estimates of the TREM and GTREM frontier models. Statistics are based on the full sample of observations.

**Figure 2:** Development of estimated cost efficiencies over time.

*Note:* Figure 2 presents the development of estimated cost efficiencies under the TREM and GTREM specification. For every individual year, firm level cost efficiency estimates are separated into quartiles. The figure shows the development of the yearly mean values of these quartiles.

The TREM and the persistent efficiency component of the GTREM measure different sorts of cost efficiency. Hence, the correlation between these two estimated efficiency levels is low and even negative (cf. Table 5). Accordingly, the correlation between the persistent and transient efficiency estimates of the GTREM is negative as well. In contrast, the correlation between the TREM cost efficiency and the transient efficiency of the GTREM is, as expected, positive and comparatively high. Therefore, it can be concluded that firms showing a high degree of persistent efficiency are not contemporaneously exhibiting production processes of a high degree of transient efficiency. In conclusion, the GTREM is our preferred model specification, because it allows for a simultaneous estimation of the level of persistent as well as transient cost efficiency. The predicted aggregate level of cost inefficiency of this model amounts to 22.3 percent (7.9 percent transient, 14.4 percent persistent) on average.

**Table 5:** *Correlation coefficients of the efficiency estimates.*

|                  | TREM | GTREM persistent | GTREM transient  |
|------------------|------|------------------|------------------|
| TREM             | 1    | -0.180 [-0.071*] | 0.844 [0.763*]   |
| GTREM persistent |      | 1                | -0.647 [-0.499*] |

*Note:* This table presents the correlation coefficients between estimated efficiencies of the TREM and GTREM frontier models. Spearman correlations are given in [.] brackets. Asterisks \* indicate significance at a level of 5 percent.

### 5.3 Economies of Density and Scale

The estimated coefficients reported in Table 3 can be used to compute the firms' level of economies of density and scale. Following the pioneering work of Caves, Christensen et al. (1981) and Caves, Christensen et al. (1984), economies of density (ED) and economies of scale (ES) are estimated as

$$ED = \frac{1}{\partial \ln C / \partial \ln Y},$$

$$ES = \frac{1}{\partial \ln C / \partial \ln Y + \partial \ln C / \partial N}.$$

Economies of scale differ to economies of density (sometimes also called economies of spatial scale) in the assumption that an increase in firm size not only raises output, but to the same proportion also the number of plants under operation (Farsi, Filippini et al., 2005). Economies of density and scale exist if the respective values of ED and ES are greater than 1. Analogously, values smaller than 1 indicate diseconomies of density or scale.

**Table 6:** *Economies of density (ED) and scale (ES) of the sample.*

|    |                          | TREM  | GREM  |
|----|--------------------------|-------|-------|
| ED | 1 <sup>st</sup> quartile | 1.579 | 1.675 |
|    | Median                   | 2.018 | 2.035 |
|    | 3 <sup>rd</sup> quartile | 2.626 | 2.586 |
| ES | 1 <sup>st</sup> quartile | 1.047 | 0.969 |
|    | Median                   | 1.179 | 1.107 |
|    | 3 <sup>rd</sup> quartile | 1.558 | 1.543 |

*Note:* This table presents the economies of density and scale when using estimates of the TREM and GTREM frontier models. Statistics are based on the respective first, second and third quartile firm observation.

**Table 7:** Economies of density (ED) and scale (ES) of three typical firms.

|    |        | TREM  | GREM  |
|----|--------|-------|-------|
| ED | Small  | 1.627 | 1.619 |
|    | Medium | 2.002 | 2.061 |
|    | Large  | 2.565 | 2.694 |
| ES | Small  | 1.433 | 1.398 |
|    | Medium | 1.237 | 1.172 |
|    | Large  | 1.195 | 1.124 |

*Note:* This table presents the economies of density and scale when using estimates of the TREM and GTREM frontier models. Statistics are based on first, second and third quartile typical firms.

Table 6 illustrates the descriptive statistics of the economies of scale and density computed for all firms in our sample and Table 7 presents the values for a small, medium and large hydropower firm. A small firm for instance is defined by values of  $Y$  and  $N$  that correspond to the first quartiles of the distribution of each variable. Accordingly, for the medium firm we use the median values of  $Y$  and  $N$  and for the large firm we use the respective third quartile values. The results reported in the two tables confirm the existence of positive economies of density and scale for most firms.<sup>20</sup>

## 6 Conclusions and Discussion

The goal of this paper was to estimate the persistent and transient cost efficiency levels in the Swiss hydropower sector applying two distinct frameworks: a true random effects

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<sup>20</sup> The study of Filippini and Luchsinger (2007) yields similar results. They estimate the economies of scale (but not economies of density) in the Swiss hydropower sector for the period 1995 to 2002 and find these scale economies to amount to 1.76 for small, 1.78 for medium and 1.76 for large firms.

model (TREM) and generalized true random effects model (GTREM). From a methodological point of view, the GTREM model seems to be interesting because it allows to simultaneously measure both types of efficiency, i.e. the persistent and transient one. The GTREM predicts the aggregate level of cost inefficiency to amount to 22.3 percent (7.9 percent transient, 14.4 percent persistent) on average between 2000 and 2013.

Results show that the Swiss hydropower sector is characterized by the presence of both, transient as well as persistent, cost inefficiencies. These inefficiencies are different in absolute value and the negative correlations between them indicate that they indeed measure two kinds of inefficiencies, which differ in interpretation and implication. The transient component represents cost inefficiencies varying with time, e.g., inefficiencies stemming from a wrong adaptation of production processes towards changing factor prices or singular management mistakes. On the other hand, the persistent part captures cost inefficiencies which do not vary with time, like inefficiencies due to recurring identical management mistakes, unfavorable boundary conditions for electricity generation or factor misallocations difficult to change over time.

The two types of cost efficiency allow a firm to elicit its cost saving potential in the short- as well as the long-run, but they might require a firm's management to respond with different improvement strategies. From a regulatory point of view, the results of this study could be used in the scope and determination of the amount of subsidies to be granted to a hydropower firm. Knowledge of the level of cost efficiency supports the government in avoiding a grant of subsidies to inefficient hydropower firms. If a hydropower firm shows a high level of cost inefficiency, then the amount of the subsidy should be reduced or cancelled completely. However, the regulatory authority

should differentiate between persistent and transient levels of efficiency also consider inertia in the short run possibilities of hydropower firms to ameliorate the level of persistent efficiency.

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# A Appendix: testing for monotonicity and quasi-concavity

Linear homogeneity in factor prices of the cost function given in eq. (2) implies

$$c(Y, \lambda P_L, \lambda P_W, \lambda P_K, \lambda P_E) = \lambda c(Y, P_L, P_W, P_K, P_E) \mid \lambda > 0.$$

To reduce notation, unit  $i$  and time  $t$  subscripts are dropped. Homogeneity is imposed by dividing total costs and factor prices by the price of energy. Hence, what remains to be tested is the monotonicity and quasi-concavity of the cost function. Given the cost function of eq. (2), the estimated cost share equations are

$$\begin{aligned} \frac{\partial \ln C}{\partial \ln P_L} &= \hat{S}_L = \hat{\beta}_l + \hat{\beta}_{ll} p_l + \hat{\beta}_{lw} p_w + \hat{\beta}_{lk} p_k, \\ \frac{\partial \ln C}{\partial \ln P_W} &= \hat{S}_W = \hat{\beta}_w + \hat{\beta}_{ww} p_w + \hat{\beta}_{lw} p_l + \hat{\beta}_{wk} p_k, \\ \frac{\partial \ln C}{\partial \ln P_K} &= \hat{S}_K = \hat{\beta}_k + \hat{\beta}_{kk} p_k + \hat{\beta}_{lk} p_l + \hat{\beta}_{wk} p_w. \end{aligned}$$

Monotonicity is ensured if total costs are increasing in input prices as well as in output, i.e. if the following four conditions hold

$$\frac{\partial \ln C}{\partial \ln Y} = \hat{\beta}_y + \hat{\beta}_{yy} y + \sum_{z=\{F,n\}} \hat{\beta}_{yz} z > 0 \text{ and } \hat{S}_L > 0 \text{ and } \hat{S}_W > 0 \text{ and } \hat{S}_K > 0. \quad (3)$$

Results of the evaluation of monotonicity at the sample's mean and median are shown in Table 8. The results obey the restrictions noted in eq. (3).

Concavity is given if the Hessian matrix of second order partial derivatives is negative semidefinite. According to Binswanger (1974) p. 380 the second order partial derivatives of a cost function can be derived as

$$\frac{\partial^2 C}{\partial P_i \partial P_j} = \frac{C}{P_i P_j} (\beta_{ij} + S_i \cdot S_j) \text{ and } \frac{\partial^2 C}{\partial P_i^2} = \frac{C}{P_i^2} (\beta_{ii} + S_j^2 - S_j), \text{ where } i, j = \{L, W, K, E\}.$$

**Table 8: Monotonicity at sample mean and median.**

|                                      | TREM  | GTREM |
|--------------------------------------|-------|-------|
| <b>Monotonicity at sample mean</b>   |       |       |
| $\hat{S}_L$                          | 0.053 | 0.726 |
| $\hat{S}_W$                          | 0.168 | 0.079 |
| $\hat{S}_K S$                        | 0.636 | 0.158 |
| $\partial \ln C / \partial \ln Y$    | 0.753 | 0.659 |
| <b>Monotonicity at sample median</b> |       |       |
| $\hat{S}_L$                          | 0.058 | 0.675 |
| $\hat{S}_W$                          | 0.171 | 0.082 |
| $\hat{S}_K$                          | 0.628 | 0.162 |
| $\partial \ln C / \partial \ln Y$    | 0.698 | 0.653 |

*Note:* This table presents the estimated cost shares as well as the first derivative of total costs with respect to output of the TREM and GTREM frontier models evaluated at the sample mean or median.

Hence, at the approximation point<sup>21</sup> (the median), the Hessian matrix becomes

$$\mathbf{G} = \begin{bmatrix} \hat{\beta}_{ll} + \hat{\beta}_l^2 - \hat{\beta}_l & \hat{\beta}_{lw} + \hat{\beta}_l \cdot \hat{\beta}_w & \hat{\beta}_{lk} + \hat{\beta}_l \cdot \hat{\beta}_k & \hat{\delta}_{le} + \hat{\beta}_l \cdot \hat{\delta}_e \\ \hat{\beta}_{lw} + \hat{\beta}_w \cdot \hat{\beta}_l & \hat{\beta}_{ww} + \hat{\beta}_w^2 - \hat{\beta}_w & \hat{\beta}_{wk} + \hat{\beta}_w \cdot \hat{\beta}_k & \hat{\delta}_{we} + \hat{\beta}_w \cdot \hat{\delta}_e \\ \hat{\beta}_{lk} + \hat{\beta}_k \cdot \hat{\beta}_l & \hat{\beta}_{wk} + \hat{\beta}_k \cdot \hat{\beta}_w & \hat{\beta}_{kk} + \hat{\beta}_k^2 - \hat{\beta}_k & \hat{\delta}_{ke} + \hat{\beta}_k \cdot \hat{\delta}_e \\ \hat{\delta}_{le} + \hat{\delta}_e \cdot \hat{\beta}_l & \hat{\delta}_{we} + \hat{\delta}_e \cdot \hat{\beta}_w & \hat{\delta}_{ke} + \hat{\delta}_e \cdot \hat{\beta}_k & \hat{\delta}_{ee} + \hat{\delta}_e^2 - \hat{\delta}_e \end{bmatrix}.$$

The  $\delta$ -coefficients are not estimated directly, due to the a priori imposition of the homogeneity assumption. However, given the linear homogeneity constraints, they can be derived as

$$\begin{aligned} \hat{\delta}_e &= 1 - \hat{\beta}_l - \hat{\beta}_w - \hat{\beta}_k, \\ \hat{\delta}_{le} &= 0 - \hat{\beta}_{ll} - \hat{\beta}_{lw} - \hat{\beta}_{lk}, \\ \hat{\delta}_{we} &= 0 - \hat{\beta}_{ww} - \hat{\beta}_{lw} - \hat{\beta}_{wk}, \\ \hat{\delta}_{ke} &= 0 - \hat{\beta}_{kk} - \hat{\beta}_{lk} - \hat{\beta}_{wk}, \\ \hat{\delta}_{ee} &= 0 - \hat{\delta}_{le} - \hat{\delta}_{we} - \hat{\delta}_{ke}. \end{aligned}$$

The vector of fitted factor shares is

$$\mathbf{s} = \begin{bmatrix} \hat{S}_L \\ \hat{S}_W \\ \hat{S}_K \\ \hat{S}_E \end{bmatrix},$$

where  $\hat{S}_E = 1 - \hat{S}_L - \hat{S}_W - \hat{S}_K$ . The cost function is concave if the roots of the matrix  $\mathbf{H} = \mathbf{G} + \mathbf{s} \cdot \mathbf{s}' - \text{diag}(\mathbf{s})$  are non-positive, e. if  $\lambda_i \leq 0 \forall i = 1, \dots, 4$  with  $\det(\mathbf{H} - \lambda \cdot \mathbf{I}_4) = 0$ .

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<sup>21</sup> At the approximation point, all second order and interaction terms of a translog function collapse to zero.

The roots of matrix  $\mathbf{H}$  evaluated at the sample's mean and median are given in Table 9. In subsection 5.1 a justification is given for this slight violation of the concavity condition.

**Table 9:** *Roots of matrix  $\mathbf{H}$  at sample mean and median.*

|                                   | TREM         | GTREM        |
|-----------------------------------|--------------|--------------|
| <b>Concavity at sample mean</b>   |              |              |
| $\lambda_1$                       | <i>0.429</i> | <i>0.202</i> |
| $\lambda_2$                       | -0.000       | -0.000       |
| $\lambda_3$                       | -0.159       | -0.184       |
| $\lambda_4$                       | -0.406       | -0.419       |
| <b>Concavity at sample median</b> |              |              |
| $\lambda_1$                       | <i>0.426</i> | <i>0.201</i> |
| $\lambda_2$                       | <i>0.000</i> | -0.000       |
| $\lambda_3$                       | -0.162       | -0.187       |
| $\lambda_4$                       | -0.409       | -0.422       |

*Note:* This table presents the roots of matrix  $\mathbf{H}$  of the TREM and GTREM frontier models evaluated at the sample mean or median. Critical, i.e. positive values are given in *italics*.

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